Contents

	Prefa	ce	1	<i>page</i> iv			
1	A to	ur of tl	ne NEURON simulation environment	; 1			
	1.1	Modeling and understanding					
	1.2	Introdu	icing NEURON	2			
	1.3	State t	he question	3			
	1.4	Formul	late a conceptual model	4			
	1.5	Implen	nent the model in NEURON	6			
		1.5.1	Starting and stopping NEURON	6			
		1.5.2	Bringing up a CellBuilder	7			
		1.5.3	Entering the specifications of the model				
			cell	9			
		1.5.4	Saving the model cell	23			
		1.5.5	Executing the model specification	23			
	1.6	Instrur	nent the model	28			
		1.6.1	Signal sources	28			
		1.6.2	Signal monitors	28			
	1.7	Set up controls for running the simulation					
	1.8	Save m	odel with instrumentation and run contro	1 37			
	1.9	Run th	e simulation experiment	37			
	1.10	Analyz	e results	39			
2	The	modeli	ng perspective	47			
	2.1	Why n	nodel?	47			

Contents

	2.2	From 1	physical system to computational model	48
		2.2.1	Conceptual model: a simplified repre-	
			sentation of a physical system	48
		2.2.2	Computational model: an accurate	
			representation of a conceptual model	49
		2.2.3	An example	50
3	\mathbf{Exp}	ressing	conceptual models in mathematical	
	tern			52
	3.1	Chemi	cal reactions	52
		3.1.1	Flux and conservation in kinetic schemes	53
		3.1.2	Stoichiometry, flux, and mole equivalents	56
		3.1.3	Compartment size	57
	3.2		cal circuits	61
	3.3	Cables		69
4	Esse	entials c	of numerical methods for neural mod-	
	\mathbf{elin}	g		75
	4.1	Spatia	l and temporal error in discretized cable	
		equation	ons	76
		4.1.1	Analytic solutions: continuous in time	
			and space	77
		4.1.2	Spatial discretization	78
		4.1.3	Adding temporal discretization	82
	4.2	Numer	ical integration methods	83
		4.2.1	Forward Euler: simple, inaccurate and	
			unstable	84
		4.2.2	Backward Euler: inaccurate but stable	89
		4.2.3	Crank-Nicholson: stable and more	
			accurate	90
		4.2.4	Adaptive integration: fast or accurate,	
			occasionally both	95
	4.3	Error		109
	4.4	Summ	ary of NEURON's integration methods	112
		4.4.1	Fixed time step integrators	113
		4.4.2	Adaptive integrators	114

ii

Contents	iii
Epilogue	116
References	117
Index	120

Preface

I promise nothing complete; because any human thing supposed to be complete, must for that very reason infallibly be faulty.

Who should read this book

This book is about how to use the NEURON simulation environment to build and use empirically-based models of neurons and neural networks. It is written primarily for neuroscience investigators, teachers, and students, but readers with a background in the physical sciences or mathematics who have some knowledge about brain cells and circuits and are interested in computational modeling will also find it helpful. The emphasis is on the most productive use of NEURON as a means for testing hypotheses that are founded on experimental observations, and for exploring ideas that may lead to the design of new experiments. Therefore the book uses a problem-solving approach, with many working examples that readers can try for themselves.

What this book is, and is not, about

Formulating a *conceptual model* is an attempt to capture the essential features that underlie some particular function. This necessarily involves simplification and abstraction of real-world complexities. Even so, one may not necessarily understand all implications of the conceptual model. To evaluate a conceptual model it is often necessary to devise a hypothesis or test in which the behavior of the model is compared against a prediction. *Computational models* are useful for performing such tests. The conceptual model and the hypothesis should

Preface

determine what is included in a computational model and what is left out. This book is not about how to come up with conceptual models or hypotheses, but instead focuses on how to use NEURON to create and use computational models as a means for evaluating conceptual models.

What to read, and why

The first chapter conveys a basic idea of NEURON's primary domain of application by guiding the reader through the construction and use of a model neuron. This exercise is based entirely on NEURON's GUI, and requires no programming ability or prior experience with NEURON whatsoever.

The second chapter considers the role of computational modeling in neuroscience research from a general perspective. Chapters 3 and 4 focus on aspects of applied mathematics and numerical methods that are particularly relevant to computational neuroscience. Chapter 5 discusses the concepts and strategies that are used in NEURON to simplify the task of representing neurons, which (at least at the level of synapses and cells) are distributed and continuous in space and time, in a digital computer, where neither time nor numeric values are continuous. Chapter 6 returns to the topic of model construction, emphasizing the use of programming.

Chapters 7 and 8 provide "inside information" about NEURON's standard run and initialization systems, so that readers can make best use of their features and customize them to meet special modeling needs. Chapter 9 shows how to use the NMODL programming language to add new biophysical mechanisms to NEURON. This theme continues in Chapter 10, which starts with mechanisms of communication between cells (gap junctions, graded and spike-triggered synaptic transmission), and moves on to models of artificial spiking neurons (e.g. integrate and fire cells). The first half of Chapter 11 is a tutorial on NEURON's GUI tools for creating simple network models, and

the second half shows how to use the combined strength of the GUI and hoc programming to create more complex networks.

Chapter 12 discusses the elementary features of the hoc programming language itself. Chapter 13 describes the object-oriented extensions that have been added to hoc. These extensions have greatly facilitated construction of NEURON's GUI tools, and they can also be very helpful in many other complex programming tasks such as creating and managing network models. Chapter 14 presents an example of how to use object oriented programming to increase the functionality of NEURON.

Appendix 1 presents a mathematical analysis of the IntFire4 artificial spiking cell mechanism, proving a result that is used to achieve computational efficiency. Appendix 2 summarizes the commands for NEURON's built-in text editor.

Typeface conventions

Program listings, names of sections and density mechanisms, classes, objects, methods, procedures, functions, statements, and URLs are printed in a monospaced typeface. Optional code, or items that are generic placeholders that the reader should substitute with his or her own specific entries, are indicated by *slanted monospace*. Samples of command-line usage employ **bold monospace** to signify user input. Labels and menus that appear in NEURON's graphical interface are presented with a sans serif typeface.

Acknowledgments

First and foremost, we want to thank our mentor and colleague John W. Moore for his vision, support, encouragement, and active participation in the development of NEURON, without which neither it nor this book would exist. Through his research and teaching, he was introducing students to "computational neuroscience" long before that

Preface

glorious term was invented. NEURON had its beginnings in John's laboratory at Duke University almost three decades ago, when he and one of the authors (MLH) started their collaboration to develop simulation software for neuroscience research. Users of NEURON on the Macintosh owe John a particular debt. He continues to participate in the development and dissemination of NEURON, concentrating most recently on educational applications in collaboration with Ann Stuart(Moore and Stuart, 2000, 2007).

The list of others who have added in one way or another to the development of NEURON is far too long for this short preface. Zach Mainen, Alain Destexhe, Bill Lytton, Terry Sejnowski, and Gordon Shepherd deserve special mention for many contributions, both direct and indirect, that range from specific enhancements to the program, to fostering the wider acceptance of computational approaches in general, and NEURON in particular, by the neuroscience community at large. We also thank the countless NEURON users whose questions and suggestions continue to help guide the evolution of this software and its documentation. The development of NEURON and this book has been made possible by support from the National Institutes of Health and the National Science Foundation. We are sure that our readers will recognize the epigrams from Herman Melville's Moby Dick that are scattered throughout this book, as well as the (mis)quotation from The Treasure of the Sierra Madre (book by B. Traven, screenplay by John Huston). We hope that everyone else will forgive any omission and remind us, gently, in time for the second edition.

Finally, we thank our wives and children for their encouragement and patience while we completed this book.

A tour of the NEURON simulation environment

... so, entering, the first thing I did was to stumble over an ash-box in the porch. Ha! thought I, ha, as the flying particles almost choked me, are these ashes from that destroyed city, Gomorrah?

1.1 Modeling and understanding

Modeling can have many uses, but its principal benefit is to improve understanding. The chief question that it addresses is whether what is known about a system can account for the behavior of the system. An indispensable step in modeling is to postulate a *conceptual model* that expresses what we know, or think we know, about a system, while omitting unnecessary details. This requires considerable judgment and is always vulnerable to hindsight and revision, but it is important to keep things as simple as possible. The choice of what to include and what to leave out depends strongly on the hypothesis that we are studying. The issue of how to make such decisions is outside the primary focus of this book, although from time to time we may return to it briefly.

The task of building a *computational model* should only begin after a conceptual model has been proposed. In building a computational model we struggle to establish a match between the conceptual model and its computational representation, always asking the question: would the conceptual model behave like the simulation? If not, where are the errors? If so, how can we use NEURON to help understand why the conceptual model implies that behavior?

1.2 Introducing NEURON

NEURON is a simulation environment for models of individual neurons and networks of neurons that are closely linked to experimental data. NEURON provides numerically sound, computationally efficient tools for conveniently constructing, exercising, and managing models, so that special expertise in numerical methods or programming is not required for its productive use. Increasing numbers of experimentalists and theoreticians are incorporating it into their research strategies. As of this writing, well over 1000 scientific publications have reported work done with NEURON on topics that range from the molecular biology of voltage-gated channels to the operation of networks containing tens of thousands of neurons (see **Research reports that have used NEURON** at http://www.neuron.yale.edu/neuron/static/bib/usednrn.html).

In the following pages we introduce NEURON by going through the development of a simple model from start to finish. This will require us to perform each of these tasks:

- 1. State the question that we are interested in
- 2. Formulate a conceptual model
- 3. Implement the model in NEURON
- 4. Instrument the model, i.e. attach signal sources and set up graphs
- 5. Set up controls for running simulations
- 6. Save the model with instrumentation and run controls
- 7. Run simulation experiments
- 8. Analyze results

Since our aim is to provide an overview, we have chosen a simple model that illustrates just one of NEURON's strengths: the convenient representation of the spread of electrical signals in a branched dendritic architecture. We could do this by writing instructions in NEURON's programming language hoc, but for this example we will employ some of the tools that are provided by its graphical user interface (GUI). Later chapters examine hoc and the graphical tools for constructing models and managing simulations in more detail, as



Figure 1.1 A. Two neuronal morphologies obtained from Neuro-Morpho.org (http://neuromorpho.org/). Ca1 pyramidal cell (left, ri04 from Golding et al. (2005), scale 100 μm) and calretininpositive interneuron (right, cr20b from Gulyás et al. (1999), scale 50 μm). B. Conceptual model neuron used for the example in this chapter. The synapse can be located anywhere on the cell.

well as many other features and applications of the NEURON simulation environment (e.g. customization of the user interface, complex biophysical mechanisms, neural networks).

1.3 State the question

The scientific issue that motivates the design and construction of this model is the question of how synaptic efficacy is affected by synaptic location and the anatomical and biophysical properties of the postsynaptic cell. This has been the subject of too many experimental and theoretical studies to reference here. Interested readers will find numerous relevant publications in NEURON's on-line bibliography (cited above), and may retrieve working code for many of these from ModelDB (http://senselab.med.yale.edu/modeldb/).

1.4 Formulate a conceptual model

Most neurons have many branches with irregularly varying diameters and lengths (Fig. 1.1A), and their membranes are populated with a wide assortment of ionic channels that have different ionic specificities, kinetics, dependence on voltage and second messengers, and spatial distributions. Scattered over the surface of the cell may be hundreds or thousands of synapses, some with a direct effect on ionic conductances (which may also be voltage-dependent) while others act through second messengers. Synapses themselves are far from simple, often displaying stochastic and use-dependent phenomena that can be quite prominent, and frequently being subject to various pre- and postsynaptic modulatory effects. Given all this complexity, we might well ask if it is possible to understand anything without understanding everything. From the very onset we are forced to decide what to include and what to omit.

Suppose we are already familiar with the predictions of the basic ball and stick model (Rall, 1977; Jack et al., 1983), and that experimental observations motivate us to ask questions such as: How do synaptic responses observed at the soma vary with synaptic location if dendrites of different diameters and lengths are attached to the soma? What happens if some parts of the cell have active currents, while others are passive? What if a neuromodulator, or shift of the background level of synaptic input, changes membrane conductance?

Then our conceptual model might be similar to the one shown in Fig. 1.1B. This model includes a neuron with a soma that gives rise to an axon and two dendritic trunks, and a single excitatory synapse that may be located at any point on the cell. Although deliberately more complex than the prototypical ball and stick, the anatomical and biophysical properties of our model are much simpler than the biological original (Table 1.1). The axon and dendrites are simple cylinders, with uniform diameters and membrane properties along their lengths. The dendrites are passive, while the soma and axon have Hodgkin-Huxley (HH) sodium, potassium, and leak currents, and are capable of generating action potentials (Hodgkin and Huxley, 1952).

	$\begin{array}{c} \text{Length} \\ (\mu m) \end{array}$	$\begin{array}{c} \text{Diameter} \\ (\mu m) \end{array}$	Biophysics
Soma	30	30	HH g_{Na}, g_K , and g_{leak}
Apical dendrite	600	1	Passive with $R_m = 5000 \ \Omega \ cm^2$, $E_{pas} = -65 \ \mathrm{mV}$
Basilar dendrite	200	2	Same as apical dendrite
Axon	1000	1	Same as soma

Table 1.1 Model cell parameters

 Table 1.2 Synaptic mechanism parameters

g_{max}	$0.05 \ \mu S$
$ au_s$	$0.1 \ ms$
E_s	0 mV

A single synaptic activation causes a localized transient conductance increase with a time course described by an alpha function

$$g_s(t) = \begin{cases} 0 & t < t_{act} \\ g_{max} \frac{(t - t_{act})}{\tau_s} e^{\frac{(t - t_{act})}{\tau_s}} & t \ge t_{act} \end{cases}$$
(1.1)

where t_{act} is the time of synaptic activation, and g_s reaches a peak value of g_{max} at $t = \tau_s$ (Equation 1.1; see Table 1.2 for parameter values). This conductance increase mechanism is just slightly more complex than the ideal current sources used in many theoretical studies (Rall, 1977; Jack et al., 1983), but it is still only a pale imitation of any real synapse (Bliss and Lømo, 1973; Ito, 1989; Castro-Alamancos and Connors, 1997; Thomson and Deuchars, 1997).

1.5 Implement the model in NEURON

With a clear picture of our model in mind, we are ready to express it in the form of a computational model. Instead of writing instructions in NEURON's programming language hoc, for this example we will employ some of the tools that are provided by NEURON's graphical user interface.

We begin with the CellBuilder, a graphical tool for constructing and managing models of individual neurons. At this stage, we are not considering synapses, stimulating electrodes, or simulation controls. Instead we are focussing on creating a representation of the continuous properties of the cell. Even if we were not using the CellBuilder but instead were developing our model entirely with hoc code, it would probably be best for us to follow a similar approach, i.e. specify the biological attributes of the model cell separately from the specification of the instrumentation and control code that we will use to exercise the model. This is an example of modular programming, which is related to the "divide and conquer" strategy of breaking a large and complex problem into smaller, more tractable steps.

The CellBuilder makes it easier for us to create a model of a neuron by allowing us to specify its architecture and biophysical properties through a graphical interface. When we are satisfied with the specification, the CellBuilder will generate the corresponding hoc code for us. Once we have a model cell, we will be ready to use other graphical tools to attach a synapse to it and plot simulation results (see **1.6 Instrument the model**).

The images in the following discussion were obtained under MSWindows; the appearance of NEURON under UNIX, Linux, and OS X is quite similar.

1.5.1 Starting and stopping NEURON

No matter what a program does, the first thing you have to learn is how to start and stop it. To start NEURON under UNIX or Linux, just type nrngui on the command line and skip the remainder of this paragraph. Under MSWindows, double click on the nrngui icon on your desktop (Fig. 1.2A); if you don't see one there, bring up the NEURON program group (i.e. use Start / Program Files / NEURON) and select the nrngui item (Fig. 1.2B). If you are using OS X, open the folder where you installed NEURON and double click on the nrngui icon.

You should now see the NEURON Main Menu toolbar (Fig. 1.2C), which offers a set of menus for bringing up graphical tools for creating models and running simulations. If you are using UNIX or Linux, a "banner" that includes the version of NEURON you are running will be printed in the xterm where you typed nrngui, and the prompt will change to oc> to indicate that NEURON's hoc interpreter is running. Under OS X and MSWindows, the banner and oc> prompt will appear in a new terminal window (Fig. 1.2D).

There are three different ways to exit NEURON; use whichever is most convenient:

- 1. type D (i.e. control D) at the oc> prompt
- 2. type quit () at the oc> prompt
- click on File in the NEURON Main Menu, scroll down to Quit, and release the mouse button (Fig. 1.3)

1.5.2 Bringing up a CellBuilder

To get a CellBuilder just click on Build in the NEURON Main Menu toolbar, scroll down to the CellBuilder item, and release the mouse button (Fig. 1.4A). A CellBuilder will appear, displaying its About page which contains some useful hints (Fig. 1.4B).

Across the top of the CellBuilder is a row of radio buttons and a checkbox that correspond to the sequence of steps involved in building a model cell. Each radio button brings up a different page of the CellBuilder, and each page provides a view of the model plus a graphical interface for defining properties of the model. The **Topology**, **Subsets**, **Geometry**, and **Biophysics** pages are used to create



Figure 1.2 A and B. Under MSWindows, it is convenient to start NEURON by clicking on the nrngui icon on the desktop, or by selecting the nrngui item in the NEURON program group. C. Regardless of the operating system, the NEURON Main Menu toolbar looks and works the same. D. NEURON's banner and oc> prompt in an rxvt terminal under MSWindows.

a complete specification of a model cell. On the **Topology** page, we will set up the branched architecture of the model and give a name to each

	NEURON Main Menu							
	Iconify	(
	File	Edit	Build	Tools	Graph	Vector	Window	
1	load s	ession						
	load h	oc						
	load dll							
	save session							
	workin	g dir						
	recent	dir						
	Print							
	Quit	6						

Figure 1.3 One way to exit NEURON is to click on File / Quit in the NEURON Main Menu toolbar.

branch, without regard to diameter, length, or biophysical properties. The Subsets page is for grouping sections that share common features. Well-chosen subsets can save a lot of effort later by helping us create very compact specifications of anatomical and biophysical properties. We will deal with length and diameter on the Geometry page, and the Biophysics page is where we will define the properties of the membrane and cytoplasm of each of the branches.

1.5.3 Entering the specifications of the model cell

1.5.3.1 Topology

We start by using the **Topology** page to set up the branched architecture of the model. As Fig. 1.5 shows, when a new CellBuilder is created, it already contains a branch (or "section," as it is called in NEURON) that serves as the root of the branched architecture of the model (the root of a tree is the branch that has no parent). This root section is initially called "soma," but we can rename it if we desire (see below).

The **Topology** page offers many functions for creating and editing individual sections and subtrees. We can make the section that will become our apical dendrite by following the steps presented in



А.

CellBui	ld[0]						
Close	Hide						
🔶 About	🔷 Topology 💠 Subsets 💠 Geometry 💠 Biophysics 💠 Management 📗 Continuous Create						
Topology	refers to section names, connections, and 2d orientation						
witho	ut regard to section length or diameter.						
Short	sections are represented in that tool as circles, longer ones as lines.						
Subsets	allows one to define named section subsets as functional						
group	is for the purpose of specifying membrane properties.						
Geometr	Geometry refers to specification of L and diam (microns), and nseg						
for each section (or subset) in the topology of the cell.							
Biophysics is used to insert membrane density mechanisms and specify their parameters.							
Management specifies how to actually bring the cell into existence for simulation.							
The default is to first build the entire cell and export it to the top level							
Or else specify it as a cell type for use in networks,							
It also allows you to import the existing top level cell into this builder							
for n	for modification.						
If "Contin	If "Continuous Create" is checked, the spec is continuously instantiated						
at the	e top level as it is changed.						

В.

Figure 1.4 A. Using the NEURON Main Menu to bring up a CellBuilder. B. The About page of a CellBuilder contains some useful hints.

Fig. 1.6. Repeating these actions a couple more times (and resorting to Undo Last, Reposition, and Delete Section as needed to correct mistakes) gives us the basilar dendrite and axon.

Our model cell should now look like Fig. 1.7. At this point some



Figure 1.5 The Topology page. The left panel shows a simple diagram of the model (a "shape plot"). The buttons in the right panel are controls for editing the branched architecture of a model cell.



Click to start a new section. One end of the new

section will automatically attach to the nearest end of an existing section; the other end is tethered to the cursor while the mouse button is held down.

Drag to the desired length and orientation.

Release the mouse button.

Figure 1.6 Making a new section. Verify that the Make Section radio button is on, then perform the steps shown above.

minor changes would improve its appearance: moving the labels away from the sections so they are easier to read (Fig. 1.8), and then renaming the apical and basilar dendrites and the axon (Figs. 1.9 and 1.10). The final result should resemble Fig. 1.11.



Figure 1.7 The model after all sections have been created.



Figure 1.8 How to change the location of a label.



Basename dend

Click the Basename button.

This pops up a Section name prefix window.

Section na	me prefix:	
apical	\mathbf{k}	

Click inside the text entry field, and type the desired name. It is important to keep the mouse cursor inside the text field while typing; otherwise keyboard entries may not have an effect.

Basename: anic:	al
Basename: 🖣 ap	ic

After the new base name is complete, click on the Accept button. This closes the Section name prefix window, and the new base name will appear next to the Basename button.

Figure 1.9 Preparing to change the name of a section. Each section we created was automatically given a name based on "dend." To change these names, we must first change the base name as shown here.



Figure 1.10 Changing the name of a section.



Figure 1.11 The Subsets page. The middle panel lists the names of all existing subsets, and the right panel has controls for managing subsets. In the shape plot, the sections that belong to the currently selected subset are shown in red. When the Subsets page initially appears, it already has an all subset that contains every section in the model.

1.5.3.2 Subsets

The Subsets page deserves special comment. In almost every model that has more than one branch, two or more branches will have at least some biophysical attributes that are identical, and there are often significant anatomical similarities as well. Furthermore, we can almost always apply the d_lambda rule for compartmentalization throughout the entire cell (see below). Subsets allow us to take advantages of such regularities by assigning shared properties to several branches at once. The Subsets page (Fig. 1.11) is where we group branches into subsets, on the basis of shared features, with an eye to exploiting these commonalities on the Geometry and Biophysics pages. This allows us to create a model specification that is compact, efficient, and easily understood.

The properties of the sections in this particular example suggest that we create two subsets: one that contains the basilar and apical branches, which are passive, and another that contains the soma and axon, which have Hodgkin-Huxley (HH) spike currents. To make a subset called has_HH that contains the sections with HH currents, follow the steps in Fig. 1.12. Then make another subset called no_HH that contains the basilar and apical dendrites.

1.5.3.3 Geometry

In order to use the Geometry page (Fig. 1.13) to specify the anatomical dimensions of the sections and the spatial resolution of our model, we must first set up a strategy for assigning these properties. After we have built our (hopefully efficient) strategy, we will give them specific values.

The geometry strategy for our model is simple. Each section has different length L and diameter diam, so the properties of each section must be entered individually. As far as the spatial resolution of the model is concerned, for this model (and most others) the best choice is to let NEURON automatically determine the spatial discretization of each section based on a fraction of the length constant at 100 Hz (spatial accuracy and NEURON's tools for adjusting the spatial grid



Figure 1.12 Making a new subset.

are discussed in **Chapter 5**). Figure 1.14 shows how to set up this strategy.

Having set up the strategy, we are ready to assign the geometry parameters (Fig. 1.15). At the top of the list is d_lambda. By specifying that spatial discretization will follow the d_lambda rule, we have



Figure 1.13 When the Geometry page in a new CellBuilder is first viewed, a red check mark should appear in the Specify Strategy checkbox. If not, click on the checkbox to toggle Specify Strategy on.

stipulated that NEURON will automatically discretize the model, breaking each section into just enough compartments so that none is longer than d_lambda times the AC length constant at 100 Hz. The default value of d_lambda is 0.1, i.e. 10% of the AC length constant. This is short enough for most purposes, so we do not need to change it.

Scrolling through the other geometry parameters reveals that the default values of many lengths and diameters differ from our desired specification (cf. Table 1.1). Figure 1.16 shows how to change soma length to 30 μm . After all revisions have been made, the geometry parameters should look like Fig. 1.17. Note the x in the middle panel, which signifies that one or more parameters associated with the adjacent section or subset name have been altered. In the right panel, note the red marks in checkboxes; these identify the parameters that have been changed from their default values.



Figure 1.14 Specifying strategy for assignment of geometry parameters. First make sure that Specify Strategy contains a red check (see Fig. 1.13). For models in which the geometry of each section is unique, like this one, click on the L and diam boxes under "Distinct values over subset." To allow NEURON to take care of spatial discretization automatically, click on the d_lambda box under "Spatial Grid."



Figure 1.15 Assigning values to the geometry parameters. Toggling Specify Strategy off makes the middle panel show the subsets and sections that we selected when setting up our strategy. Our strategy is based entirely on the all subset, so all is the only item that appears in the middle panel. The buttons in the right panel display the names of the sections and parameters that are associated with the all subset, and offer us the means to change parameters as necessary. The vertical scroll bar along the right edge indicates that some buttons fall below the bottom edge of the CellBuilder's window; these can be revealed by dragging the scroll bar up or down.



To set the length of the soma to $30 \ \mu m$, first click inside the numeric field for soma.L so that a red editing cursor appears.



Then use the backspace key to delete the old value, type in the new value, and press "Enter" on your keyboard. The red mark in the checkbox indicates that this parameter has been changed from its default value.

Figure 1.16 Assigning values to the geometry parameters continued.



Figure 1.17 The revised geometry parameters. The x in the middle panel and the red marks in the right panel signal changes from default values.



Figure 1.18 The Biophysics page, ready for specification of strategy. The right panel shows the mechanisms that are available to be inserted into our model. For this simple example, the number of mechanisms is deliberately small; adding new mechanisms is covered in **Chapter 9**.



Figure 1.19 Specifying strategy for assignment of biophysical parameters. First make sure that **Specify Strategy** contains a red check, then proceed with the steps described above.

1.5.3.4 Biophysics

The Biophysics page (Fig. 1.18) is used to specify the biophysical properties of membrane and cytoplasm (e.g. Ra, Cm, ion channels, buffers, pumps) for subsets and individual sections. As with the Geometry page, first we set up a strategy, then we review and adjust parameter values. After we have applied the steps outlined in Figs. 1.19 and 1.20, the CellBuilder will contain a complete specification of our model.

📕 Specify Strategy	forsec all { // specify Ra
all	Ra (ohm-cm) 💅 100 🖕 🔶
x Ra	h)
cm	
has_HH	
hh	
no_HH	
pas	

For the all subset, change Ra from its default 35.4 $\Omega\,cm$ to the desired 100 $\Omega\,cm$.

📕 Specify Strategy	forsec no_HH { insert pas
all	g_pas (S/cm2) 0.001
x Ra cm	e_pas (m∨) 🗾 -70 🔶
has_HH hh	
_no_HH	
pas	

The sections in the no_HH subset have a passive current whose parameters must be changed from their defaults (shown here).



The value of g_pas can be set by deleting the default value, then typing 1/5000(= 1/Rm).

📕 Specify Strategy	forsec no_HH { insert pas
all x Ra cm has HH hh no_HH x pas	g_pas (S/cm2)

The final values of g_pas and e_pas. Not shown: cm (all subset) and the parameters of the hh mechanism (has_HH subset), which have the desired values by default and do not need to be changed, although it is good practice to review them.

Figure 1.20 Assigning values to the biophysical parameters. Toggling **Specify Strategy** off shows a list of the names of the subsets that are part of the strategy. Beneath each subset are the names of the mechanisms that are associated with it. Clicking on a mechanism name brings up controls in the right panel for displaying and adjusting its parameters.

1.5 Implement the model in NEURON

1.5.4 Saving the model cell

Having invested time and effort to set up our model, we would be wise to take a moment to save it. The CellBuilder, like NEURON's other graphical tools, can be saved to disk as a "session file" for future re-use, as shown in Figs. 1.21 and 1.22. For more information about saving and retrieving session files, including how to use the Print & File Window Manager GUI tool to select and save specific windows, see Using Session Files for Saving and Retrieving Windows at http://www.neuron.yale.edu/neuron/static/docs/saveses/ saveses.html

1.5.5 Executing the model specification

Now that the CellBuilder contains a complete specification of the model cell, we could use the Export button on the Management page (see Chapter 6) to write out a hoc file that, when executed by NEU-RON, would create the model. However, for this example we will just turn Continuous Create on (Fig. 1.23). This makes the CellBuilder send its output directly to NEURON's interpreter without bothering to write a hoc file. The model cell whose specifications are contained in the CellBuilder is now available to be used in simulations.

If we make any changes to the model while Continuous Create is on, the CellBuilder will automatically send new code to the interpreter. This can be very convenient during model development, since it allows us to quickly examine the effects of any change. Automatic updates might bog things down if we were dealing with a large model on a slow machine. In such a case, we could just turn Continuous Create off, make whatever changes were necessary, and then cycle it on and off again.



Figure 1.21 A. To save all of NEURON's graphical windows to a session file, first click on File in the NEURON Main Menu and scroll down to save session. B. This brings up a directory browser that can be used to navigate to the directory where the session file will be saved. C. Click in the edit field at the top of the directory browser and type the name to use for the session file, then click on the Save button.



Figure 1.22 A. To recreate the graphical windows that were saved to a session file, first click on File in the NEURON Main Menu and scroll down to load session. B. Use the directory browser that appears to navigate to the directory where the session file was saved. Then double click on the session file that you want to retrieve.



Figure 1.23 Using Continuous Create.

NEURON Main Menu Iconify						_ 🗆	×
File	Edit	Build	Tools	Graph	Vecto	r Windo	w
			RunControl RunButton VariableStepControl Parallel Computing Point Processes Distributed Mechanisms				Point Manager
		I	Fitting Impedan Model VI Movie Ru Miscella	iew Jn			Electrode

Figure 1.24 Bringing up a PointProcessManager in order to attach a synapse to our model cell. In the NEURON Main Menu, click on Tools / Point Processes / Managers / Point Manager, then proceed as shown in Fig. 1.25



Figure 1.25 Configuring a new PointProcessManager to emulate a synapse. A. Note the labels in the top panel. None means that a signal source has not yet been created. The bottom panel shows a stick figure of our model cell. B. SelectPointProcess / Al-phaSynapse creates a point process that emulates a synapse with a conductance change governed by Eq. 1.1, and shows us a panel for adjusting its parameters.

1.6 Instrument the model

1.6.1 Signal sources

In the NEURON simulation environment, a synapse or electrode for passing current (current clamp or voltage clamp) is represented by a point source of current which is associated with a localized conductance. Such localized signal sources are called "point processes" to distinguish them from properties that are distributed over the cell surface (e.g. membrane capacitance, active and passive ionic conductances) or throughout the cytoplasm (e.g. buffers), which are called "distributed mechanisms" or "density mechanisms."

We have already seen how to use one of NEURON's graphical tools for dealing with distributed mechanisms (the CellBuilder). To attach a synapse to our model cell, we turn to one of NEURON's tools for dealing with point processes: the PointProcessManager (Fig. 1.24). Using a PointProcessManager we can specify the type and parameters of the point process (Fig. 1.25) and where it is attached to the cell.

1.6.2 Signal monitors

Since one motivation for the model is to examine how synaptic responses observed at the soma vary with synaptic location, we want a graph that shows the time course of somatic membrane potential. In the laboratory this would ordinarily require attaching an electrode to the soma, so in a NEURON simulation it might seem to require a point process. However, the computer automatically evaluates somatic V_m in the course of a simulation. In other words, graphing V_m doesn't really change the system, unlike attaching a signal source, which adds new equations to the system. This means that a point process is not needed; instead, we just bring up a graph that includes somatic V_m in the list of variables that it plots (see Fig. 1.27).

We could monitor V_m at other locations by adding more variables to this graph, and bring up additional graphs if this one became too crowded. However, it can be more informative and convenient to


The top panel of the

PointProcessManager indicates what kind of point process has been specified, and where it is located (in this case, at the midpoint of the soma). The bottom panel shows the parameters of an AlphaSynapse: its start time onset and time constant tau (t_{act} and τ_s in Eq. 1.1), peak conductance gmax (g_{max} in Eq. 1.1), and reversal potential e (E_s in Table 1.2). The button marked i (nA) is just a label for the adjacent numeric field, which displays the instantaneous synaptic current.

For this example change onset to 0.5 ms and gmax to 0.05 μS ; leave tau and e unchanged.

Figure 1.26 Specifying the properties of an AlphaSynapse.

create a "space plot". A space plot is a Graph in which a variable is plotted as a function of distance along one or more branches of a cell. Figures 1.28-1.30 show how to set up a space plot of membrane potential that can change throughout a simulation, displaying the evolution of V_m as a function of space and time.



Figure 1.27 Creating a graph to display somatic membrane potential as a function of time.



Figure 1.28 The first step in setting up a space plot is to create a Shape object, which is used to specify the space plot's path. A. To create a Shape, click on Graph / Shape plot in the NEURON Main Menu. B. This brings up a Shape window, which can be used to set up graphs of a range variable-membrane potential (v) in this case-vs. time or distance. C. Click on the menu box in the Shape window to bring up its primary menu. While still depressing the mouse button, scroll down the menu to the Space Plot item, then release the button. The Shape window is now ready to be used to specify the space plot's paths.



Place the cursor just to the left of the distal end of the axon and press the left mouse button.

While still holding the button down, drag the cursor across the window to the right, finally releasing the button when the cursor has passed the distal end of the apical dendrite.

The branches along the selected path (axon, soma, and apical dendrite) are now shown in red, and a new window pops up that shows a space plot of v along this path (see Fig. 1.30). At this point, you may click on the Close button at the upper left corner of the Shape window to conserve screen space.

Figure 1.29 Specifying a space plot's paths.



Figure 1.30 The space plot of membrane potential created by the steps shown in Figs. 1.28 and 1.29. The x axis shows the distance from the 0 end of the default section, which in this example is the left end of the soma.



Β.

Figure 1.31 A. To bring up a window with controls for running simulations, click on the RunControl button in NEU-RON Main Menu / Tools. B. The RunControl provides many options for controlling the overall time course of a simulation run.

1.7 Set up controls for running the simulation

At this point we have a model cell with a synapse attached to the soma, and a graphical display of somatic V_m . All that is missing is a means to start and control the subsequent course of a simulation run. This is provided by a RunControl panel (Fig. 1.31), which offers a great deal of control over simulations.

Of the many options that this tool allows us to specify, these three are most relevant to this example:

1. Init (mV) sets time t to 0, assigns the displayed starting value (-65 mV) to V_m throughout the model cell, and sets the ionic conductances to their their steady state values at this potential.

- 2. Init & Run performs the same initialization as Init (mV), and then starts a simulation run.
- Points plotted/ms determines how often the graphical displays are updated during a simulation.

Three other items in this panel are of obvious interest, although we will not do anything with them for now. The first is dt, which sets the size of the time intervals at which the equations that describe the model are solved. The second is **Tstop**, which specifies the duration of a simulation run. Finally, the button marked t doesn't actually do anything but is just a label for the adjacent numeric field, which displays the elapsed simulation time. Additional features of the RunControl panel are discussed in **Chapter 7**.

The last item to add to our user interface is a Movie Run tool, as shown in Fig. 1.32. We will use this tool to launch simulations in which the space plot of membrane potential evolves smoothly.



Α.

Figure 1.32 A. To bring up a tool for running simulations that update space plots smoothly, click on the Movie Run button in NEURON Main Menu / Tools. B. Clicking on the Init & Run button in the Movie Run tool starts a simulation in which space plots are refreshed at intervals specified by the value shown in the the Seconds per step field.

1.8 Save model with instrumentation and run control

After some rearrangement, our customized user interface for running simulations and observing simulation results should look something like Fig. 1.33. For the sake of safety and possible future convenience, it is a good idea to use NEURON Main Menu / File / save session to save this custom GUI to a session file.

1.9 Run the simulation experiment

We are now ready to use our "virtual experimental rig" to exercise the model. Clicking on the lnit & Run button in the RunControl panel (Fig. 1.34) launches a simulation, and the graph of somatic membrane potential vs. time shows that the synaptic input triggers a spike at that location (Fig. 1.35).

To examine how V_m evolves throughout the cell, let us now turn to the space plot. If a simulation is launched with RunControl's lnit & Run button, NEURON takes the time-saving shortcut of deferring shape plot updates until the end of the run. Consequently our shape plot only shows the distribution of V_m at the end of the simulation. In order to see the shape plot evolve over the course of the simulation, it is necessary to click on the Movie Run tool's lnit & Run button. This makes NEURON update the shape plot at each new time step, and reveals how the spike starts at the soma and spreads out to the axon and apical dendrite (Fig. 1.36).

The utility of the space plot as a tool for understanding the spatiotemporal evolution of a variable can be enhanced by using it like a storage oscilloscope (Figs. 1.37 and 1.38; also see Fig. 1.39 for how to erase "stored" traces). This can make it easier to evaluate and compare the spatial distribution of variables at successive intervals during a run.

NEURON's GUI greatly simplifies the task of constructing and using models. In particular, the GUI makes it easy to perform experi-



Figure 1.33 Our user interface for running simulations and observing results. Other windows that are present on the screen but not shown in this figure are the NEURON Main Menu and the CellBuilder.

mental manipulations of a model and see what happens. For example, we can explore the effect of changing the location of the synaptic input. If we move the synapse even a small distance away from the



Figure 1.34 Running a simulation. The response to an excitatory synaptic input at the soma is shown in Figs. 1.35, 1.36, and 1.38.



Figure 1.35 The excitatory synapse at the soma elicits a somatic spike.

soma along the apical dendrite (Fig. 1.40) and run a new simulation, the epsp at the soma is too small to evoke a spike (Fig. 1.41).

1.10 Analyze results

In this section we turn from our specific example to a consideration of the analysis of results. Models are generally constructed either for



Figure 1.36 Snapshots of simulation results taken at 1 ms intervals. Each pair of graphs shows V_m vs. distance and V_m at the soma (v(.5)) vs. t. Synaptic input at the soma triggers a spike that propagates actively along the axon and spreads with passive decrement into the apical dendrite.

didactic purposes or as a means for testing a hypothesis. Both the design and analysis of any model are strongly dependent on this original motivation, which determines what features are included in the model, what variables are regarded as important enough to measure, and how these measurements are to be interpreted.

While computational models are arguably simpler than any (interesting) experimental preparation, analysis of simulation results presents its own special problems. In the first place, attempting to use

40



Figure 1.37 Preparing to capture "multiple exposures" of the spatial distribution of V_m .

a digital computer to mimic the behavior of a biological system introduces many potential complexities and artifacts. Some arise from



Now clicking on Init & Run in the Movie Run tool generates a set of traces that facilitate examination of impulse initiation and propagation through the model.

For this example the synapse was at the middle of the soma (soma(0.5)). Before running another simulation with a different synaptic location, it would be a good idea to erase these traces (see Fig. 1.39).

Figure 1.38 Capturing "multiple exposures" of the spatial distribution of $V_m.$

the fact that neurons are continuous in space and time, but a digital computer can only generate approximate solutions for a finite number of discrete locations at particular instants. Even so, under the right conditions the approximation can be very good indeed. Furthermore, a well-designed simulation environment can reduce the difficulty of achieving good results.

Other difficulties can arise if there is a mismatch between the expectations of the user and the level of detail that has been included in a model. For example, the most widely used computational model of a conductance change synapse is designed to do the same thing each and every time it is "activated," yet most real synapses display many kinds of use-dependent plasticity, and many also have a high degree of stochastic variability. And even the venerable Hodgkin-Huxley model (1952), which is probably *the* classical success story of computational neuroscience, does not replicate all features of the action potential in the squid giant axon, because it does not completely capture the



Bring up the primary graph menu and scroll down to **Erase**.



When the mouse button is released, all traces vanish but one: the trace that that shows the current values of V_m along the path.

Figure 1.39 How to erase traces.

dynamics of the currents that generate the spike (Moore and Cox, 1976; Fohlmeister et al., 1980; Clay and Shlesinger, 1982). Such discrepancies are potentially a problem only if a user who is unaware of their existence attempts to apply a model outside of its original context.

The first analysis that is required of all computational modeling is actually the verification that what has been implemented in the computer is a faithful representation of the conceptual model. At the least, this involves checking to be sure that the intended anatom-



Show

In the top panel of the PointProcessManager, click on Show and scroll down to Shape.

The top panel remains unchanged, but the bottom panel of the PointProcessManager now displays a shape plot of the cell, with a blue dot that indicates the location of the synapse.

Clicking on a different point in the shape plot moves the synapse to a new location. This change is reflected in the top and bottom panels of the PointProcessManager.

Figure 1.40 Changing synaptic location.

ical and biophysical features have been included, that parameters have been assigned the desired values, and that appropriate initialization and integration methods have been chosen. It may also be necessary to test the model's biophysical mechanisms to ensure that they show the correct dependence on time, membrane potential, ionic concentrations, and modulators. This means understanding the internals of the computational model, which in turn demands a nontrivial grasp of the programming language in which it is expressed. A custom graphical interface that includes well-designed menus and "variable browsers" can make it easier to answer the frequently occurring question "what are the names of things?" Even so, every simulation environment is predicated on a set of underlying concepts and assumptions, and questions inevitably arise that can only be answered on the basis of knowledge of these core concepts and assumptions.

Verification should also involve the qualitative, if not quantitative, comparison of simulation results with basic predictions obtained



Figure 1.41 Pressing Init & Run starts a new simulation. Even though the synapse is still quite close to the soma, the somatic depolarization is now too small to trigger a spike (space plot not shown).

from experimental observations on biological preparations or generated with prior models. Discrepancies between prediction and simulation are usually caused by trivial errors in model implementation, but sometimes the fault lies in the prediction. Detecting these more interesting outcomes requires practical facility with the simulation environment, so that the level of effort does not obscure one's thinking about the problem.

Agreement between prediction and simulation is reassuring and suggests that the model itself may be useful for generating experimentallytestable predictions. Thus the effort shifts from verifying the model to characterizing its behavior in ways that extend beyond the initial test runs. Both verification and characterization of neural models may entail determining not only membrane potential but also rate functions, levels of modulators, and ionic conductances, currents, and concentrations at one or more locations in one or more cells. Thus it is necessary to be able to gather and manage measurements, both within a single simulation run and across a family of runs in which one or more independent variables are assigned different values.

Similar concerns arise in connection with optimization, in which

one or more parameters are adjusted until the behavior of the model satisfies certain criteria. Optimization also opens a host of new questions whose answers depend in part on the user's judgment, and in part on the resources provided by the simulation environment. Which parameters should remain fixed and which should be adjustable? What constitutes a "run" of the model? What are the criteria for goodness of fit? What constraints, if any, should be imposed on adjustable parameters, and what rules should govern how they are adjusted?

In summary, analysis of results can be the most difficult aspect of any experiment, whether it was performed on living neurons or on a computer model, yet it can also be the most rewarding. The issues raised here are critical to the informed use of any simulation environment, and in the following chapters we will reexamine them in the course of learning how to develop and exercise models with NEURON.

The modeling perspective

. . . can you not tell water from air? My dear sir, in this world it is not so easy to settle these plain things. I have ever found your plain things the knottiest of all.

This chapter and the next deal with concepts that are not NEURONspecific but instead pertain equally well to *any* tools used for neural modeling.

2.1 Why model?

In order to achieve the ultimate goal of understanding how nervous systems work, it will be necessary to know many different kinds of information:

- the anatomy of individual neurons and classes of cells, pathways, nuclei, and higher levels of organization
- the pharmacology of ion channels, transmitters, modulators, and receptors
- the biochemistry and molecular biology of enzymes, growth factors, and genes that participate in brain development and maintenance, perception and behavior, learning and forgetting, health and disease

But while this knowledge will be necessary for an understanding of brain function, it isn't sufficient. This is because the moment-tomoment processing of information in the brain is carried out by the spread and interaction of electrical and chemical signals that are distributed in space and time. These signals are generated and regulated by mechanisms that are kinetically complex, highly nonlinear, and arranged in intricate anatomical structures. Hypotheses about these signals and mechanisms, and how nervous system function emerges from their operation, cannot be evaluated by intuition alone, but require empirically-based modeling. From this perspective, modeling is fundamentally a means for enhancing insight, and a simulation environment is useful to the extent that it maximizes the ratio of insight obtained to effort invested.

2.2 From physical system to computational model

Just what is involved in creating a computational model of a physical system?

2.2.1 Conceptual model: a simplified representation of a physical system

The first step is to formulate a *conceptual model* that attempts to capture just the essential features that underlie a particular function or property of the physical system. If the aim of modeling is to provide insight, then formulating the conceptual model necessarily involves simplification and abstraction (Fig. 2.1 left). When a physical system is already simple enough to understand, there is no point in further simplification because we won't learn anything new. If instead the system is complex, a conceptual model that omits excess detail can foster understanding.

But some models contain essential irreducible complexities, and even conceptual models that are superficially simple can resist intuition. To evaluate such a model it is often necessary to devise a hypothesis or test in which the behavior of the model is compared against a prediction. *Computational models* are useful for performing such tests. The conceptual model, and the hypothesis behind it, determine what is included in the computational model and what is left out.



Figure 2.1 Creating a computational model of a physical system involves two steps. The first step deliberately omits real-world complexities to produce a conceptual model. In the second step, this conceptual model must be faithfully translated into a computational model, without any further subtractions or additions.

When we formalize our description of a biological system, the first language we use is mathematics. The conceptual model is usually expressed in mathematical form, although there are occasions when it is more convenient to express the concept in the form of a computer algorithm. **Chapter 3** is concerned with mathematical representations of chemical and electrical phenomena relevant to signaling in neurons.

2.2.2 Computational model: an accurate representation of a conceptual model

A computational model is a working embodiment of a conceptual model through the medium of computer simulation. It can assist hypothesis testing by serving as a virtual laboratory preparation in which the functional consequences of the hypothesis can be examined. Such tests can be valid only if the computational model is as faithful to the conceptual model as possible. This means that the computational model must be implemented in a way that does not impose additional simplifications or introduce new properties that were not consciously chosen by the user; otherwise how can the user tell whether simulation results truly reflect the properties of the conceptual model, and are not a byproduct of distortions produced by trying to implement the model with a computer? This ideal is impossible to achieve, and the proper use of any simulator requires judgment by the user as to whether discrepancies between concept and concrete representation are benign or vicious. A useful simulation environment enables experimental tests of hypotheses by facilitating the construction, use, and revision of computational models that are faithful to the original idea and its subsequent evolution. NEURON is designed to meet this goal, and one of the aims of this book is to show you how to tell whether the model you have in mind is matched by the NEURON simulation you create.

2.2.3 An example

Figure 2.2A shows the side view of a Ca1 pyramidal neuron. Suppose we are interested in how this cell responds to current injected at the soma. We could imagine an enormously complicated conceptual model that attempts to mimic all of the detail of the physical system. But if we are trying to gain insight into the charging properties of the cell as observed at the soma, we might start with a much simpler conceptual model, like the ball and stick shown in Fig. 2.2B. Most of the anatomical complexity of the physical system lies in the dendritic tree, but our conceptual model approximates the entire dendritic tree by a very simple abstraction: a cylindrical cable.

So going from the physical system to the model involved simplification and abstraction. What about going from the conceptual model to a computational model? The statements in Fig. 2.2C specify the topology of the computational model hoc, NEURON's built-in programming language. Note that everything in the conceptual model has a direct counterpart in this computational implementation, and vice versa: the transition between concept and computational model involves neither simplification nor additional complexity. All that remains is to assign physical dimensions and biophysical properties, and the computational model can be used to generate simulations that reflect the behavior of the conceptual model.



Figure 2.2 A. Side view of Cal pyramidal neuron (ri04 from Golding et al. (2005), data available at http://neuromorpho.org/). B. "Ball and stick" conceptual model. C. Computational implementation of the conceptual model.

References

- Bliss, T.V.P., and Lømo, T. 1973. Long-lasting potentiation of synaptic transmission in the dentate area of the anaesthetised rabbit following stimulation of the perforant path. *Journal of Physiology*, 232, 331– 356.
- Brown, P.N., Hindmarsh, A.C., and Petzold, L.R. 1994. Using Krylov methods in the solution of large-scale differential-algebraic systems. SIAM Journal of Scientific Computing, 15, 1467–1488.
- Carslaw, H.S., and Jaeger, J.C. 1980. Conduction of Heat in Solids. 2 edn. Oxford: Oxford University Press.
- Castro-Alamancos, M.A., and Connors, B.W. 1997. Distinct forms of shortterm plasticity at excitatory synapses of hippocampus and neocortex. Proceedings of the National Academy of Sciences of the United States of America, 94, 4161–4166.
- Clay, J.R., and Shlesinger, M.F. 1982. Delayed kinetics of squid axon potassium channels do not always superpose after time translation. *Biophysical Journal*, **37**, 677–680.
- Cohen, S.D., and Hindmarsh, A.C. 1994. *CVODE User Guide*. Tech. rept. URCL-MA-118618. Lawrence Livermore National Laboratory.
- Cohen, S.D., and Hindmarsh, A.C. 1996. CVODE, a stiff/nonstiff ODE solver in C. Computers in Physics, 10, 138–143.
- Crank, J. 1979. *The Mathematics of Diffusion*. 2 edn. London: Oxford University Press.
- Crank, J., and Nicholson, P. 1947. A practical method for numerical evaluation of solutions of partial differential equations of the heat-conduction type. Proceedings of the Cambridge Philosophical Society, 43, 50–67.
- Dahlquist, G., and Bjorck, A. 1974. Numerical Methods. Englewood Cliffs, New Jersey: Prentice-Hall.

- Fohlmeister, J.F., Adelman, W.J.Jr., and Poppele, R.E. 1980. Excitation properties of the squid axon membrane and model systems with current stimulation. *Biophysical Journal*, **30**, 79–97.
- Golding, N.L., Mickus, T.J., Katz, Y., Kath, W.L., and Spruston, N. 2005. Factors mediating powerful voltage attenuation along CA1 pyramidal neuron dendrites. *Journal of Physiology-London*, 568(1), 69–82.
- Gulyás, A.I., Megías, M., Emri, Z., and Freund, T.F. 1999. Total number and ratio of excitatory and inhibitory synapses converging onto single interneurons of different types in the CA1 area of the rat hippocampus. *Journal of Neuroscience*, **19**, 10082–97.
- Hamming, R.W. 1987. Numerical Methods for Scientists and Engineers. 2 edn. Dover Publications.
- Hindmarsh, A.C., and Serban, R. 2002. User documentation for CVODES, an ODE solver with sensitivity analysis capabilities. Tech. rept. UCRL-MA-148813. Lawrence Livermore National Laboratory.
- Hindmarsh, A.C., and Taylor, A.G. 1999. User documentation for IDA, a differential-algebraic equation solver for sequential and parallel computers. Tech. rept. UCRL-MA-136910. Lawrence Livermore National Laboratory.
- Hines, M. 1984. Efficient computation of branched nerve equations. International Journal of Bio-Medical Computation, 15, 69–76.
- Hines, M.L., and Carnevale, N.T. 1997. The NEURON simulation environment. Neural Computation, 9, 1179–1209.
- Hines, M.L., and Carnevale, N.T. 2001. NEURON: a tool for neuroscientists. *The Neuroscientist*, 7, 123–135.
- Hodgkin, A.L., and Huxley, A.F. 1952. A quantitative description of membrane current and its application to conduction and excitation in nerve. *Journal of Physiology*, **117**, 500–544.
- Ito, M. 1989. Long-term depression. Annual Review of Neuroscience, 12, 85–102.
- Jack, J.J.B., Noble, D., and Tsien, R.W. 1983. Electric Current Flow in Excitable Cells. London: Oxford University Press.
- Kundert, K. 1986. Sparse matrix techniques. In: Ruehli, Albert (ed), *Circuit Analysis, Simulation and Design.* North-Holland.
- Mainen, Z.F., and Sejnowski, T.J. 1996. Influence of dendritic structure on firing pattern in model neocortical neurons. *Nature*, 382, 363–366.
- Moore, J.W., and Cox, E.B. 1976. A kinetic model for the sodium conductance system in squid axon. *Biophysical Journal*, 16, 171–192.
- Moore, J.W., and Stuart, A.E. 2000. Neurons in Action: Computer Simulations with NeuroLab. Sunderland, MA: Sinauer Associates.

References

- Moore, J.W., and Stuart, A.E. 2007. *Neurons in Action 2: Tutorials and Simulations using NEURON*. Sunderland, MA: Sinauer Associates.
- Nilsson, J.W., and Riedel, S.A. 1996. *Electric Circuits*. 5 edn. Reading, MA: Addison-Wesley.
- Press, W.H., Teukolsky, S.A., Vetterling, W.T., and Flannery, B.P. 1992. Numerical Recipes in C. 2 edn. Cambridge: Cambridge University Press.
- Rall, W. 1964. Theoretical significance of dendritic tree for input-output relation. Pages 73–97 of: Reiss, R.F. (ed), Neural Theory and Modeling. Stanford: Stanford University Press.
- Rall, W. 1977. Core conductor theory and cable properties of neurons. Pages 39–98 of: Kandel, E. R. (ed), *Handbook of Physiology, vol. 1, part 1: The Nervous System.* Bethesda, MD: American Physiological Society.
- Stewart, D., and Leyk, Z. 1994. Meschach: Matrix Computations in C. Vol. 32. Canberra, Australia: School of Mathematical Sciences, Australian National University.
- Strang, G. 1986. Introduction to Applied Mathematics. Wellesley, MA: Wellesley-Cambridge Press.
- Thomson, A.M., and Deuchars, J. 1997. Synaptic interactions in neocortical local circuits: dual intracellular recordings in vitro. *Cerebral Cortex*, 7, 510–522.

absolute error, 85, 95, 96 local, 99 tolerance, 100, 104 abstraction, 48, 50 accuracy, 49, 86 effect of boundary conditions, 74 physiological, 104, 111 quantitative, 90 vs. speed, 97 active transport, 58 AlphaSynapse, 27 AlphaSynapse parameters, 29 amplifier, 63 gain, 63, 68 headstage, 67 analysis, 39 approximation, 42, 50, 71, 72 of a continuous system by a discrete system, 81 artificial spiking cell, 107, 108 under CVODE, 115 assumptions, 1, 57, 59, 63, 65, 70, 73 atol, 104 axial current, 71, 72, 74, 76 positive current convention, 71 axial resistance, 72, 73 backward Euler method, 82, 89, 90 iteration coefficient, 83 local error, 90, 109 stability, 89 summary, 113 ball and stick, 50

biophysical neuron model, 107 boundary conditions, 70 sealed end, 74, 77 branched architecture, 69, 72 BREAKPOINT block SOLVE sparse, 113 buffer, 53 cable, 69 branched, 72 passive cylindrical, 76, 77, 79, 81 unbranched, 69, 73, 74 calcium amount of, 58 concentration, 59 free, 105 pump, 58, 105 CellBuilder **Biophysics** page assigning values, 22 specifying strategy, 21 Geometry page assigning values, 19 specifying strategy, 18 Subsets page all subset, 14 making a new subset, 16 Topology page base name, 13 changing the name of a section, 14 making a new section, 11 CellBuilder, 6

Biophysics page, 21 bringing up, 7 Continuous Create, 23 Geometry page, 15 d_lambda, 16 Management page, 23 Export, 23 root section, 9, 30 Subsets page, 15 Topology page, 9 Basename, 13 channel, 73 conductance, 72 density, 110 gating model, 113 HH type, 93 under CVODE, 115 ligand-gated, 52 linear, 113 model, 52 nonlinear, 113 under CVODE, 115 voltage-gated, 52 charge, 69 conservation, 70, 72 circuit, 61 analysis, 61 branch, 62 edge, 62 element, 63 amplifier, 63 capacitor, 63 current source, 63 ground, 63 resistor, 63 voltage source, 63 wire, 63 equivalent, 67, 73 node, 62 parallel RC, 62 positive current convention, 62 closed system, 53, 54, 57 cm, 21, 22 compartment, 53, 71, 81 adjacent, 73, 76 size, 53, 57, 59, 71 compartmentalization, 15, 17 complexity, 47, 48, 50 computational efficiency, 91, 93, 94, 96-98, 107, 113, 115

and STATES, 107 concentration, 53, 57, 59 and accuracy, 114 gradient, 69 conductance slope, 94 conservation law, 69 Crank-Nicholson method, 82, 90, 92 - 96hybrid of backward and forward Euler, 90 iteration coefficient, 83 local error, 91, 109 kinetic scheme, 113 stability, 92 staggered time steps, 94-96 summary, 113 unstaggered time steps, 94, 95 current, 62 density, 71, 73 electrode, 67, 68, 71 source, 71, 72 current clamp, 67 CVODE, 96, 97, 99, 101, 102, 106, 107 and model descriptions, 115 default error criteria, 105 local error, 99, 104 summary, 115 CVode class record(), 108 cytoplasmic resistivity, 21, 73, 76 d_lambda rule, 15 d lambda default value, 17 DASPK, 97, 99 summary, 115 density, 53, 59 DERIVATIVE block and CVODE, 115 detail, 48, 50 how much, 1, 42 diam, 15 diameter, 4 diffusion, 58 under CVODE, 115 directory browser, 24, 25 discrepancy between conceptual model and computational model, 49

between physical system and conceptual model, 43 between prediction and simulation, 42.45 discrete event simulation, 108, 115 conditions for, 108, 115 discretization, 16, 42, 70, 76 spatial, 70, 72, 74 temporal, 70 distributed mechanism, 21, 28 $\Delta t, 83, 85, 86, 89, 91, 93, 94$ dt, 35 $\Delta x, 78, 81, 83$ eigenfunction, 88, 89 eigenvalue, 66, 88 elapsed simulation time, 35 electrode capacitance, 66 compensation, 66 resistance, 66 equation algebraic, 52, 98, 113, 114 cable, 69, 73 analytic solution, 77 characteristic, 62 current balance, 62, 64 difference, 70 differential, 52, 53, 55, 56, 59, 60, 64, 66, 69, 84, 88 coupled vs. independent, 88, 94 ordinary, 64, 72 partial, 69 sacred runes, 112 event, 106, 114 delivery, 106 input, 106 logical, 106 extracellular mechanism, 76, 99, 114 feedback amplifier, 67 capacitor, 67 positive, 67 flux, 53, 55, 56, 59 backward, 56 forward, 56 focus cursor, 13 forward Euler method, 82

iteration coefficient, 83 local error, 86, 109 stability, 83, 86 Fourier theory, 77 frequency, 88 spatial, 77, 78, 81, 83 function continuous of space, 69 of time, 69 delta, 71 discrete, 101 piecewise linear, 102, 103, 105 gap junction under CVODE, 115 Gaussian elimination, 98 good programming style divide and conquer, 6 modular programming, 6 Graph creating space plot, 31, 32 voltage axis, 30 Graph primary menu Erase, 43 Keep Lines, 41 graph theory, 61 Hamming, R.W., 112 hh mechanism, 22 hoc, 2, 23 hypothesis, 1, 40 testing, 48, 49 initial value problem, 66 initialization, 34, 44 membrane potential, 34 insight, 48, 50, 112 instrumentation, 6, 28 integrate and fire, 108, 115 intuition, 48 ion accumulation under CVODE, 115 ion channel, 21 ionic conductance, 28 iteration coefficient, 83 equation, 82 Jacobian approximate, 98

judgment, 1, 46, 49, 112 KINETIC block and CVODE, 115 kinetic scheme, 52, 53 compartment size, 57 conservation rules, 55 equivalent differential equations, 54 Kirchhoff's current law, 62 L, 15 length, 4 length constant, 15, 17 linear algebra, 87 linear circuit, 76, 99, 114 mass, 69 material, 53 amount, 53, 59 concentration, 53 conservation, 52 density, 53 membrane area, 71 membrane capacitance, 72 membrane current capacitive, 72 ionic, 72 positive current convention, 71 membrane potential, 28, 30, 67, 73 isopotential, 73 membrane resistance, 22 model ball and stick, 50 computational, 1, 6, 48, 49 analysis, 39 implementation, 49, 50 model specification, 23 conceptual, 1, 4, 43, 48, 52 model specification, 6, 23 modeling, 97, 104 empirically-based, 48, 82 rationale, 48 mole equivalents, 56 Movie Run. see NEURON Main Menu: Tools: Movie Run neurite, 70 NEURON starting and exiting, 6 NEURON Main Menu File load session, 25 save session, 24, 37

Graph Shape plot, 31 Voltage axis, 30 Tools Movie Run. 36 Point Processes, 26 RunControl, 34 NEURON Main Menu, 7 Build CellBuilder, 7 NEURON program group, 7 nrngui, 7 numeric integration, 44, 76, 83 adaptive, 95, 114 global time step, 106–108, 115 local time step, 98, 106, 107, 115 switching to fixed time step, 114 analytic integration of channel states, 94 explicit, 84, 113 fixed time step, 100, 113 event aggregation, 108 switching to adaptive, 114 implicit, 84, 113 instability, 83, 86 iteration of nonlinear equations, 93, 113order of accuracy, 94, 99, 109 stability, 98, 112 effect of signal sources, 88, 112 summary, 112 numerical error, 109 chaotic system, 110 control, 84, 104 $\Delta t, 88$ global, 101, 109 local, 86, 91, 99, 109 oscillations, 90, 92 roundoff, 87 spatial, 76, 81 temporal, 76 effect of spatial discretization, 81 Nyquist sampling theorem, 78 Ohm's law, 72 optimization, 45 oscilloscope, 37 parameters biophysical, 21, 22 geometry, 18, 19

sensitivity to, 110 pas mechanism, 21 e_pas, 22 q_pas, 22 PFWM, see Print & File Window Manager physical system, 48 representing by a model, 48, 50 point process, 28 PointProcessManager configuring as AlphaSynapse, 27, 29 creating, 26 location changing, 44 SelectPointProcess, 27 PointProcessManager, 28 location, 29, 44 parameters, 29 Show Shape, 44 prediction, 48 Print & File Window Manager, 23 qualitative results, 90 Ra, 21, 22 default value, 22 rate constant, 54 relative error local, 99, 104 tolerance, 99 RunControl creating, 34, 36 RunControl, 34 dt, 35 Init, 34 Init & Run, 34 Points plotted/ms, 35 t. 35 Tstop, 35 running a simulation, 39 scale factor, 60 secondorder, 113 section, 9 currently accessed default section, 30, 33 nodes zero area, 98 root section, 9 session file, 23

loading from NEURON Main Menu, 25 from Print & File Window Manager, 23 saving from NEURON Main Menu, 24 from Print & File Window Manager, 23 Shape creating, 31 primary menu Space Plot, 31 shape plot, 11, see also NEURON Main Menu: Graph: Shape plot shell, 58 signal chemical, 69 electrical, 69 signal monitors, 28 vs. signal sources, 28 signal sources, 28 simplification, 48-50 simulation running, 39 starting, 39 time, 35 simulation control, 6, 34 simulation environment utility of, 48, 50 space, 29, 31, 32, 42, 47 space plot, 29, 33, 35 creating, 31, 32 spatial accuracy second order, 78 spatial grid, 78 specific membrane capacitance, 21, 73, 76specific membrane conductance, 76 squid axon, 42 standard run system fadvance(), 108state, 53, 55, 57, 58 as amount of material, 53 as concentration, 53 as density, 53 as probability, 53 state variable, 89, 94, 97 stoichiometry, 56 storage oscilloscope, 37 surface area, 72

124

synapse AlphaSynapse, 27 conductance change, 27 synaptic plasticity, 108 system continuous, 75, 77-79, 81, 82 discretized, 78, 81, 82 linear, 87, 94, 113 nonlinear, 94, 113 stiff, 88, 97, 112-114 system equations effect of signal sources, 28 matrix form, 96 extracellular field, 98 linear circuit, 98 t, 34, 39 Taylor's series, 89, 109 temporal accuracy empty, 114 time, 29, 34, 39, 42, 47 time constant, 66 topology, 8, 50 understanding, 47, 48 units, 53 consistency, 56, 59, 60 user interface as virtual experimental rig, 37 custom GUI, 37, 44 user's intent, 108 v. 30 variable browser, 44 variables independent, 45 Vector class play(), 101 under adaptive integration, 102, 103under fixed time step integration, 102, 103 with interpolation, 103 verification, 43 $V_m, 28$ voltage, 62 gradient, 69 voltage clamp ramp clamp, 101 what are the names of things?, 44