Computational Neuroscience

Lab 11:

Evolutionary optimization of parameters





Instructor: Salvador Dura-Bernal

Overview

- □ Why do we need it? Examples:
 - Single cell params
 - Network firing rates
 - Behavioral performance
- Approaches
 - Hand tuning
 - Brute force
 - Search Algorithms
- Evolutionary algorithms
- Mutation rates and elites
- Optimizing the firing rate of a network



☐ Finding the optimum parameter values to achieve a target

Target typically based on experimental data, e.g.:

- Single cell intrinsic properties (f-I curve, ...)
- Network properties (firing rates, oscillations,...)
- Behavioral task (hand distance to target, ...)

Parameters of model adjusted within realistic range, e.g.:

- Density of ionic channels
- Connection weights, background inputs
- Reinforcement learning interval

Parameter optimization: cell



Parameters: Capacitance, leak, Ra, and density of channels HCN, Kd, Na, Kdr, Ka, Ca, KCa

Target: Firing rates (I-f curve), spike shape, subthreshold voltage shape



Parameter optimization: network

Parameters: Connection weights and background input rate

Target: Avg firing rates, coefficient of variation, LFP spectra, PSTH



Parameter optimization: behavior

Parameters: Training metaparameters (RL interval, exploratory movements, ...)

Target: Final distance to target, distance from ideal trajectory



Parameter optimization

3 main approaches

- Hand tuning:
 - Example: Purkinje cell (1994), 1 year of work
 - Intelligent and focused but limited search of parameter sp

Brute force

- Incomplete or complete but sparse sampling
- Computation, storage and analysis challenges
- Search algorithms
 - Find "best model" based on some *fitness* measure
 - Many methods: gradient descent, simulated annealing, genetic/ evolutionary algorithms, ...







Evolutionary Algorithms





Some individuals born happen to have longer necks due to genetic differences.

Reproduction



Individuals pass on their traits to next generation.



Over many generations, longer-necked individuals are more successful, perhaps because they can feed on taller trees, and pass the long-neck trait on to their offspring.

b. Darwin's theory: natural selection or genetically-based variation leads to evolutionary change.

Evolutionary/genetic algorithms

Mimics biology: successive generations of a population become fitter through selection, combined with mating and mutation.



Evolutionary algorithms



Evolutionary algorithms



Inspyred

- Python library for bio-inspired algorithms
- Includes evolutionary algorithms and many others
- Each stage of the algorithm is customizable
- <u>http://pythonhosted.org/inspyred/index.html</u>
- Installation: pip install inspyred

inspyred: Bio-inspired Algorithms in Python

- Overview
 - Bio-inspired Computation
 - Design Methodology
 - Installation
 - Getting Help
- Tutorial
 - The Rastrigin Function
 - The Generator
 - The Evaluator
 - The Evolutionary Computation
 - Evolving Polygons
 - The Generator
 - The Evaluator
 - The Bounder
 - The Observer
 - The Evolutionary Computation
 - Lunar Explorer
 - The Generator
 - The Evaluator
 - The Evolutionary Computation
- Examples
 - Standard Algorithms
 - Genetic Algorithm
 - Evolution Strategy
 - Simulated Annealing
 - Differential Evolution Algorithm
 - Estimation of Distribution Algorithm
 - Pareto Archived Evolution Strategy (PAES)
 - Nondominated Sorting Genetic Algorithm (NSGA-II)
 - Particle Swarm Optimization
 - Ant Colony Optimization
 - Customized Algorithms
 - Custom Evolutionary Computation
 - Custom Archiver
 - Custom Observer
 - Custom Replacer
 - Custom Selector
 - Custom Terminator
 - Custom Variator

Inspyred



Problem-specific components

- A generator that defines how solutions are created
- An **evaluator** that defines how fitness values are calculated for solutions

Algorithm-specific evolutionary operators

- A **terminator** that determines whether the evolution should end
- A selector that determines which individuals should become parents
- A **variator** that determines how offspring are created from existing individuals
- A **replacer** that determines which individuals should survive into the next generation

Inspyred example

Rastrigin example



Inspyred example

Bastrigin example

The Rastrigin function is a non-convex function used as a performance test problem for optimization algorithms.

Finding the minimum of this function is a fairly difficult problem due to its large search space and its large number of local minima.



Fitness function:

Minimize

$$10n + \sum_{i=1}^{n} \left((x_i - 1)^2 - 10\cos(2\pi(x_i - 1)) \right)$$

for $x_i \in [-5.12, 5.12]$.

Parameters: x₁, x₂



```
rand = Random()
rand.seed(int(time()))
my_ec = ec.EvolutionaryComputation(rand)
```

- Create evolutionary computation object that encapsulates the components of a generic evolutionary computation.
- These components are the *selection* mechanism, *the variation* operators, the *replacement* mechanism, the *terminators*, and the *s*.
- Requires random value since needs to generate random crossover and mutations

my_ec.selector = ec.selectors.tournament_selection

Select which parents will reproduce

inspyred.ec.selectors.uniform_selection(random, population, args)
Return a uniform sampling of individuals from the population.

This function performs uniform selection by randomly choosing members of the population with replacement.

Optional keyword arguments in args:

• num_selected - the number of individuals to be selected (default 1)

 $inspyred.ec.selectors.tournament_selection(random, population, args) \P$

Return a tournament sampling of individuals from the population.

This function selects num_selected individuals from the population. It selects each one by using random sampling without replacement to pull tournament_size individuals and adds the best of the tournament as its selection. If tournament_size is greater than the population size, the population size is used instead as the size of the tournament.

Optional keyword arguments in args:

- num_selected the number of individuals to be selected (default 1)
- tournament_size the tournament size (default 2)

inspyred.ec.selectors.truncation_selection(random, population, args)

Selects the best individuals from the population.

This function performs truncation selection, which means that only the best individuals from the current population are selected. This is a completely deterministic selection mechanism.

Optional keyword arguments in args:

• num_selected - the number of individuals to be selected (default len(population))



Terms: Crossover/Recombination

Select variations to apply during reproduction (crossover+mutation)

inspyred.ec.variators.uniform_crossover(random, candidates, args) ¶

Return the offspring of uniform crossover on the candidates.

This function performs uniform crossover (UX). For each element of the parents, a biased coin is flipped to determine whether the first offspring gets the 'mom' or the 'dad' element. An optional keyword argument in args, ux_bias, determines the bias.

Optional keyword arguments in args:

- crossover_rate the rate at which crossover is performed (default 1.0)
- ux_bias the bias toward the first candidate in the crossover (default 0.5)

inspyred.ec.variators.n_point_crossover(random, candidates, args)

Return the offspring of n-point crossover on the candidates.

This function performs n-point crossover (NPX). It selects n random points without replacement at which to 'cut' the candidate solutions and recombine them.

Optional keyword arguments in args:

- crossover_rate the rate at which crossover is performed (default 1.0)
- num_crossover_points the number of crossover points used (default 1)

Terms: Mutation

 Select variations to apply during reproduction (crossover+mutation)

inspyred.ec.variators.gaussian_mutation(random, candidates, args)

Return the mutants created by Gaussian mutation on the candidates.

This function performs Gaussian mutation. This function makes use of the bounder function as specified in the EC's evolve method.

Optional keyword arguments in args:

- *mutation_rate* the rate at which mutation is performed (default 0.1)
- gaussian_mean the mean used in the Gaussian function (default 0)
- gaussian_stdev the standard deviation used in the Gaussian function (default 1)

The mutation rate is applied on an element by element basis.

inspyred.ec.variators.scramble_mutation(random, candidates, args)

Return the mutants created by scramble mutation on the candidates.

This function performs scramble mutation. It randomly chooses two locations along the candidate and scrambles the values within that slice.

Optional keyword arguments in args:

• *mutation_rate* – the rate at which mutation is performed (default 0.1)

The mutation rate is applied to the candidate as a whole (i.e., it either mutates or it does not, based on the rate).

my_ec.replacer = ec.replacers.steady_state_replacement

Terms: Replacement

Select what set of parents and children to keep for next generation



inspyred.ec.replacers.steady_state_replacement(random, population, parents, offspring, args)

Performs steady-state replacement for the offspring.

This function performs steady-state replacement, which means that the offspring replace the least fit individuals in the existing population, even if those offspring are less fit than the individuals that they replace.

inspyred.ec.replacers.generational replacement(random, population, parents, offspring, args)

Performs generational replacement with optional weak elitism.

This function performs generational replacement, which means that the entire existing population is replaced by the offspring, truncating to the population size if the number of offspring is larger. Weak elitism may also be specified through the num_elites keyword argument in args. If this is used, the best num_elites individuals in the current population are allowed to survive if they are better than the worst num elites offspring.

Optional keyword arguments in args:

num elites – number of elites to consider (default 0)

my_ec.terminator = ec.terminators.evaluation_termination

Select criteria to stop evolutionary optimization

inspyred.ec.terminators.evaluation_termination(population, num_generations, num_evaluations, args)
Return True if the number of function evaluations meets or exceeds a maximum.

This function compares the number of function evaluations that have been generated with a specified maximum. It returns True if the maximum is met or exceeded.

Optional keyword arguments in args:

• max_evaluations - the maximum candidate solution evaluations (default len(population))

inspyred.ec.terminators.generation_termination(population, num_generations, num_evaluations, args)

Return True if the number of generations meets or exceeds a maximum.

This function compares the number of generations with a specified maximum. It returns True if the maximum is met or exceeded.

Optional keyword arguments in args:

• max_generations – the maximum generations (default 1)

 Select what information to observe/display during the evolutionary computations Generation Evaluation Median Average 450 1000 16.4311490 0.09074930 0.10785487 0.47232884 1.62516803 Best Individual: [1.0207958718596968, 0.9949433488753152] : 0.0907493057544 80 average 70 median 60 best worst 50 Fitness 40 30 20 10

600

800

1000

inspyred.ec.observers.stats_observer(population, num_generations, num_evaluations, args)

Print the statistics of the evolutionary computation to the screen.

This function displays the statistics of the evolutionary computation to the screen. The output includes the generation number, the current number of evaluations, the maximum fitness, the minimum fitness, the average fitness, and the standard deviation.

0

200

400

Evaluations

inspyred.ec.observers.best_observer(population, num_generations, num_evaluations, args)

Print the best individual in the population to the screen.

This function displays the best individual in the population to the screen.

inspyred.ec.observers.plot_observer(population, num_generations, num_evaluations, args)

Plot the output of the evolutionary computation as a graph.

This function plots the performance of the EC as a line graph using the pylab library (matplotlib) and numpy. The graph consists of a blue line representing the best fitness, a green line representing the average fitness, and a red line representing the median fitness. It modifies the keyword arguments variable 'args' by including an entry called 'plot_data'.

• Select prpperties of evolutionary algorithm





Understanding population size

Start from lab10_optim1.py (Rastrigin example) make the following changes:

1) Change the population size (pop_size) from 100 to a) 10 individual and b) 500 individuals -- what effect does it have?

Note 1: Population size is constant through generations, but only new individuals need to be evaluated; ie. all individuals are evaluated once at the beginning, but after that only offspring.

Note 2: The number of new individuals (offspring) in each generation is determined by the parameter num_selected (the number of offspring will be equal to the number of individuals selected for reproduction, ie. 1 child / parent -- not completely intuitive but that's how it works)

pop_size







- Why is 'worst' higher at start in 100 and 500?
- □ Why is 'best' lower at start in 500?
- Why is 10 faster to converge?

Understanding selection

2) Using pop_size=100, change the number of individuals selected for reproduction (num_selected) from 2 to

- a) 20 and
- b) b) 100

What is the effect?

How would the graph look if the x-axis showed num generations instead of evaluations?

num_selected







- Why do the 'worst' lines look so different?
- How would the graph look if x-axis was Generations ?

(hint: write down the total number of generations in each case)

Understanding mutation

3) Using pop_size=100 and num_selected=2, remove the gaussian_mutation variator.

What is the effect in convergence?

How does the final fitness solution compare to previous ones?

- a) What happens if you now reduce pop_size=10?
- b) Using pop_size=10, num_selected=10, put back the gaussian_mutation variator; and test the following 3 mutation_rate values: 0, 0.1 and 2 -- what's going on?

Note: This example should highlight the importance of mutation.

mutation







- □ What is the effect in convergence?
- How does the final fitness solution compare?
- Why is the effect stronger for smaller pop size?

mutation rate







Why doesn't the mut_rate=2 converge/decrease?

□ What happens when mut_rate=0?

Understanding elites

4) Using pop_size=20 and num_selected=20, mutation_rate=0.1, change the current survivor replacement method (steady_state_replacement) for the generational replacement method (http://pythonhosted.org/inspyred/reference.html#replacers-survivor-replacement-methods)

Add the argument num_elites=0 to the function call my_ec.evolve(...). Compare the output for the following values of num_elites: 0, 1 and 20.

What's the effect? Notice any difference between 0 and 1?

Note: the best *num_elites* individuals in the current population are allowed to survive if they are better than the worst *num_elites* offspring.

num elites



0

200

400

Evaluations

600

800

1000



- Why doesn't 'worst' line increase with 20 elites?
- Difference between 'best' line of 0 vs 1 elites?

Aim: optimize the network connectivity parameters to obtain a specific firing rate in the *tut2.py* example.



Target (fitness measure): mean firing rate per cell (eg. 17 Hz)

How to calculate fitness function? Minimize of maximize?

Aim: optimize the network connectivity parameters to obtain a specific firing rate in the *tut2.py* example.



Target (*fitness measure*): mean firing rate per cell (eg. 17 Hz)

Fitness = | target rate - actual rate | (minimize!)



1) We will use the network model in *tut2.py* but need to change the following things:

- Since we are going to run the model many times for each generation of the evolutionary algorithm, we don't want plots showing up for each one.

Therefore, change the simConfig options so that NO plots are generated (set plotting of raster, cells, and 2d map to False) -

- Remove the createSimulateAnalyze() call from the end of the file – we will decide when to run the model from the optimization algorithm

- Change the duration of the simulation to 0.5 sec - since we are going to run the model many times we need to make it a bit faster

2) Now lets adapt the parameter optimization code. Start from lab10_optim1.py save as lab10_optim2.py. We will begin by changing the fitness evaluation function, so it creates and runs the neural network:

- add import tut2 so we can use the network we defined there

- add from netpyne import sim so we can use netpyne to run the network

- Replace the function *evaluate_rastrigin* with *evaluate_netparams*, which should:
 - Create an empty list called *fitnessCandidates*
 - for each *candidate* create and simulate the tut2 network
 - calcualte a *fitness* value for each candidate for now just set this to a fixed value of 1 (we'll fix later)
 - Add the *fitness* if each candidate value to *fitnessCandidates*

3) In the optimizaiton algorithm options set in *my_ec.evolve*, modify the following:

- Set evaluator=evaluate_netparams so we make use of the newly defined fitness evaluator functions

- Set pop_size=10, max_evaluations=50, num_selected=10, mutation_rate=0.2

_ _ _ _

0.0

```
Creating simulation of 3 cell populations for 0.5 s on 1 hosts...
  Number of cells on node 0: 40
  Done; cell creation time = 0.00 s.
Making connections...
  Number of connections on node 0: 197
  Done: cell connection time = 0.01 s.
Running...
  Done; run time = 0.33 s; real-time ratio: 1.51.
Gathering spikes...
  Done; gather time = 0.00 s.
Analyzing...
  Run time: 0.33 s
  Simulated time: 0-s; 40 cells; 1 workers
  Spikes: 441 (22.05 Hz)
  Connections: 197 (4.92 per cell)
  Done; plotting time = 0.00 s
Total time = 0.34 s
Generation Evaluation
                           Worst
                                       Best
                                                Median
                                                          Average
                                                                      Std Dev
-----
         4
                   50
                               1
                                          1
                                                   1.0
                                                               1.0
Best Individual: [1.1721428848721431, -5.12] : 1
/u/salvadord/anaconda/lib/python2.7/site-packages/matplotlib/axes.py:2760: UserWarning:
Attempting to set identical bottom==top results
in singular transformations; automatically expanding.
bottom=1.0, top=1.0
  + 'bottom=%s, top=%s') % (bottom, top))
   1.0010
                                                    average
                                                   median
   1.0005
                                                   best
                                                   worst
Fitness
   1.0000
   0.9995
   0.9990
                  10
                             20
                                       30
                                                 40
                                                            50
        0
                              Evaluations
```

What are we missing??

0.0

```
Creating simulation of 3 cell populations for 0.5 s on 1 hosts...
  Number of cells on node 0: 40
  Done; cell creation time = 0.00 s.
Making connections...
  Number of connections on node 0: 197
  Done; cell connection time = 0.01 s.
Running...
  Done; run time = 0.33 s; real-time ratio: 1.51.
Gathering spikes...
  Done; gather time = 0.00 s.
Analyzing...
  Run time: 0.33 s
  Simulated time: 0-s; 40 cells; 1 workers
  Spikes: 441 (22.05 Hz)
  Connections: 197 (4.92 per cell)
  Done; plotting time = 0.00 s
Total time = 0.34 s
Generation Evaluation
                                                                      Std Dev
                           Worst
                                       Best
                                                Median
                                                           Average
-----
         4
                   50
                               1
                                          1
                                                   1.0
                                                               1.0
Best Individual: [1.1721428848721431, -5.12] : 1
/u/salvadord/anaconda/lib/python2.7/site-packages/matplotlib/axes.py:2760: UserWarning:
Attempting to set identical bottom==top results
in singular transformations; automatically expanding.
bottom=1.0, top=1.0
 + 'bottom=%s, top=%s') % (bottom, top))
   1.0010
                                                    average
                                                   median
   1 0005
                                                   best
                                                   worst
Fitness
   1.0000
```

0.9995

0.9990

0

10

20

Evaluations

30

40

50

What are we missing??

- Generate initial population with value within range
- Modify the network parameters based on individual evaluated
- Calculate fitness function correctly

In the main code, add a variable targetFiring to store the average target firing rate we want to obtain in the network, and set it to 18 Hz.

2) Add the minimum and maximum values for each of the 3 parameters (probability, weight and delay). These are needed during the generation of the initial population, and during the crossover and mutation phases – to make sure the genes of new children are within the allowed range:

- Create a list *minParamValues* to store minimum allowed values: 0.01 (for probability), 0.001 (for weight) and 1 (for delay)
- Create a list *maxParamValues* to store minimum allowed values: 0.5 (for probability), 0.1 (for weight) and 20 (for delay)

3) Replace the rastrigin generation function with generate_netparams using the following code:

```
def generate_netparams(random, args):
    size = args.get('num_inputs')
    initialParams = [random.uniform(minParamValues[i], maxParamValues[i]) for i in range(size)]
    return initialParams
```

Make sure you also select it in the main code: generator=generate_netparams

4) Modify the bounder (which makes sure parameter values are within the allowed range) so it makes use of the newly define parameter values: *bounder=ec.Bounder(minParamValues, maxParamValues)*; and modify the number of inputs to 3: num_inputs=3

5) Modify the tut2 network parameters (prob, weight, delay) before creating and simulating it. The parameter values (prob, weight, delay) for each new candidate/child are stored in the list *cand*:

- the probability values can be accessed via tut2.netParams.connParams]['S->M']['probability'] and should be set to cand[0]
- the probability values can be accessed via tut2.netParams.connParams['S->M']['weight'] and should be set to cand[1]
- the probability values can be accessed via tut2.netParams.connParams['S->M']['delay'] and should be set to cand[2]

6) Calculate the firing rate of the network and fitness of each individual:

- Calculate the number of spikes, by finding the length of the list containing all the spike times: *sim.simData['spkt']*
- Calculate the number of cells, by finding the length of the list contianing all the spike times: *sim.net.cells*
- Calculate the sim duration in seconds, using the *tut2.simConfig.duration* (which gives the duration in ms)
- Make sure the above values are stored as floats not integers (ie. can have decimals) to convert any value to a float use the *float(value)* function
- Calculate the average network firing rate of the network by dividing the number of spikes, by the number of cells and the duration.
- Calculate the *fitness* value for this candidate as the absolute difference (use *abs()*) between the target firing rate (use the variable we defined in prev section) and the network firing rate (just calculated above)
- Store the candidate's *fitness* value in the list *fitnessCandidates*

7) For each candidate, print a message showing the candidate number (*icand*), the 3 parameter values of the candidate (prob, weight, delay), the firing rate of the resulting candidate network, and the fitness value of the candidate network, eg.

CHILD/CANDIDATE 9: Network with prob:0.01, weight:0.00, delay:10.5 firing rate: 9.1, FITNESS = 8.95



Best Individual: [0.27529211166881334, 0.06583998948192707, 18.171594793221356] : 0.3

8) Lets now check how the network with the optimized parameters found by the evolutionary algorithm looks! At the end of the main code, add the following:

- store in *bestCand* the parameters of the best individual (optimum solution) using the following code: *final_pop.sort(reverse=True) bestCand = final_pop[0].candidate*
- Set the tut2 network parameters to those in *bestCand* (same as inside the evaluation function)
- Set the tut2 option to plot the raster: tut2.simConfig['plotRaster'] = True
- Create and simulate the tut2 network



S M

Network optimization (Assessment)

Start from *lab10_optim2.py* and replace the fitness function so that instead of the target being the average firing rate, the target is now to maximize spike synchrony (ie. the synchrony of spikes of the different cells in the network):

Add the following generic function to calculate spike synchrony.

```
def syncMeasure(spikeTimes, duration):
```

```
t0=-1
width=1
cnt=0
for spkt in spikeTimes:
if (spkt>=t0+width):
t0=spkt
cnt+=1
return 1-cnt/(duration/width)
```

- Modify the fitness evaluator function so that the fitness value for each candidate is equivalent to the synchrony of the network. Note you will need to use the *syncMeasure* above and pass the appropriate params: a list with the spike times of the network, and the duration of the simulation (you can find how to obtain both values looking at the previous examples)
- Since we want to maximize the synchrony of the network, make sure that the relevant evolutionary computation options is set to try to *maximize* the fitness (and not minimize it as before).
- Modify *tut2.py* so that you plot synchrony bars and the synchrony value for the network: *simConfig['plotSync']* = *True*

2) Replace the *delay* parameter (currently one of the 3 being optimized) with the decay time constant (*tau2*) of the network synaptic mechanism. Use the previous examples to figure out how to access this parameter in *tut2*. Set the min and max allowed values for this new parameter to 2 and 9.

3) Change the print statement for each candidate to reflect the above changes.

4) Replace the current *tournament selection* selector with *truncation selection* (only best individuals are selected).

Network optimization (Assessment)

